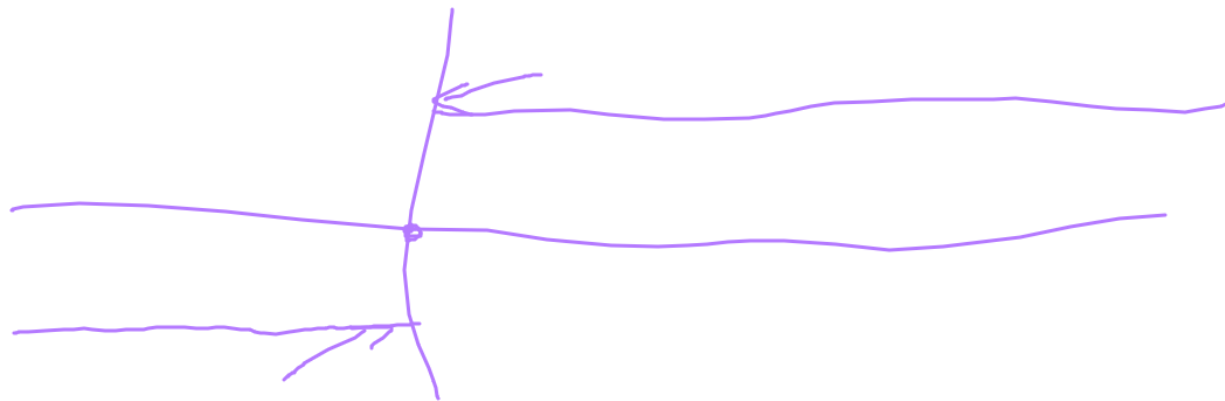


$$\lim_{x \rightarrow 1} \lfloor x \rfloor - x =$$

$$\lim_{x \rightarrow 1^-} 0 - 1 = -1$$

$$\lim_{x \rightarrow 1^+} 1 - 1 = 0$$



$$\lim_{x \rightarrow 0} \frac{(1+mx)^n - (1+nx)^m}{x^2} =$$

$$\lim_{x \rightarrow 0} \frac{1 + \cancel{nm}x + \frac{n(n-1)}{2} m^2 x^2 - \left(1 + \cancel{nm}x + \frac{m(m-1)}{2} n^2 x^2 \right)}{x^2}$$

$O(x^3)$

$$= \lim_{x \rightarrow 0} \frac{n(n-1)}{2} m^2 - \frac{m(m-1)}{2} n^2 + O(x)$$

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^k b^{n-k}$$

$$\lim_{x \rightarrow 0} \frac{x^2 - 1}{2x^2 - x - 1} = \lim_{x \rightarrow 0} \frac{1 - x^2}{1 - x - 2x^2}$$
$$= \lim_{x \rightarrow 0} \frac{1 - o(x)}{1 - o(x)}$$

$$\lim_{x \rightarrow 0} \frac{1 + 5x + x^7 - (1 + x^{10})^{10}}{x} =$$

$$= \lim_{x \rightarrow 0} \frac{\cancel{1} + 5x + x^7 - \cancel{1} - 10x^{10} - 90x^{20} - \dots}{x}$$

$$= \lim_{x \rightarrow 0} \frac{5x + x^7 + \dots}{x} = \lim_{x \rightarrow 0} \left(5 + x^6 + \dots \right)$$

$\underbrace{\hspace{10em}}_{O(x^6)}$

$$\lim_{x \rightarrow 0} e^{\frac{\sqrt[3]{1-x^2}-1}{5x^2}} = \lim_{x \rightarrow 0} e^{\frac{1-x^2-1}{5x^2(1+\sqrt[3]{1-x}+(1-x)^{\frac{2}{3}})}}$$

$$= \lim_{x \rightarrow 0} e^{\frac{1}{5(\dots)}} = e^{\frac{1}{15}}$$

$$\lim_{x \rightarrow a} \frac{f'g(x) - f'g(a)}{x-a} = \lim_{x \rightarrow a} \frac{f'(x-a)(1+f'g(x)+f'g(a))}{x-a}$$

$$= \lim_{x \rightarrow a} \frac{\sin(x-a)(1+f'g(x)+f'g(a))}{(x-a)\cos(x-a)} \stackrel{x=a+h}{=}$$

$$= \lim_{h \rightarrow 0} \frac{\sin(h)(1+f'g(a+h)+f'g(a))}{h\cos(h)} =$$

$$= \frac{1+f'g'(a)}{1}$$

$$\lim_{x \rightarrow 0} \frac{2 \ln(\cos(ax))}{2 \ln(\cos(bx))} = \lim_{x \rightarrow 0} \frac{\ln(1 - \sin^2(ax))}{\ln(1 - \sin^2(bx))}$$

$$= \lim_{x \rightarrow 0} \frac{\ln(1 + (-\sin^2(ax)))}{-\sin^2(ax)} \cdot \frac{-\sin^2(bx)}{\ln(1 + (-\sin^2(bx)))}$$

$$\frac{\sin^2(ax)}{\sin^2(bx)}$$

$$= \lim_{x \rightarrow 0} \frac{\ln(1 + (-\sin^2(ax)))}{-\sin^2(ax)} \cdot \frac{-\sin^2(bx)}{\ln(1 + (-\sin^2(bx)))}$$

$$\frac{\sin^2(ax)}{\sin^2(bx)} = \lim_{x \rightarrow 0} \frac{\sin^2(ax)}{\sin^2(bx)}$$

$$\frac{\sin^2(ax)}{(ax)^2} \cdot \frac{(bx)^2}{\sin^2(bx)} \cdot \frac{(ax)^2}{(bx)^2} = \frac{a^2}{b^2}$$

$$\begin{aligned} \lim_{x \rightarrow 0^+} (\cos(\sqrt{x}))^{\frac{1}{x}} &= \lim_{x \rightarrow 0^+} e^{\frac{1}{x} \ln(\cos(\sqrt{x}))} \\ &= \lim_{x \rightarrow 0^+} e^{\frac{1}{2x} \ln(1 - \sin^2(\sqrt{x}))} \\ &= \lim_{x \rightarrow 0^+} e^{\frac{-\sin^2(\sqrt{x})}{2x} \frac{\ln(1 - \sin^2(\sqrt{x}))}{-\sin^2(\sqrt{x})}} \end{aligned}$$

$$= \lim_{x \rightarrow 0^+} e^{-\frac{\sin^2(\sqrt{x})}{2x}} \frac{\ln(1 - \sin^2(\sqrt{x}))}{-\sin^2(\sqrt{x})}$$

$$= \lim_{x \rightarrow 0^+} e^{-\frac{1}{2} \left(\frac{\sin(\sqrt{x})}{\sqrt{x}} \right)^2} \frac{\ln(1 - \sin^2(\sqrt{x}))}{-\sin^2(\sqrt{x})}$$

$$= e^{-\frac{1}{2}}$$

$$\sum_{n=1}^{\infty} \frac{\cos(nx) - \cos((n+1)x)}{n} = \frac{\cos(nx)}{n} - \underbrace{\frac{\cos((n+1)x)}{n+1}}_{n+1} + \frac{\cos((n+1)x)}{n+1}$$

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