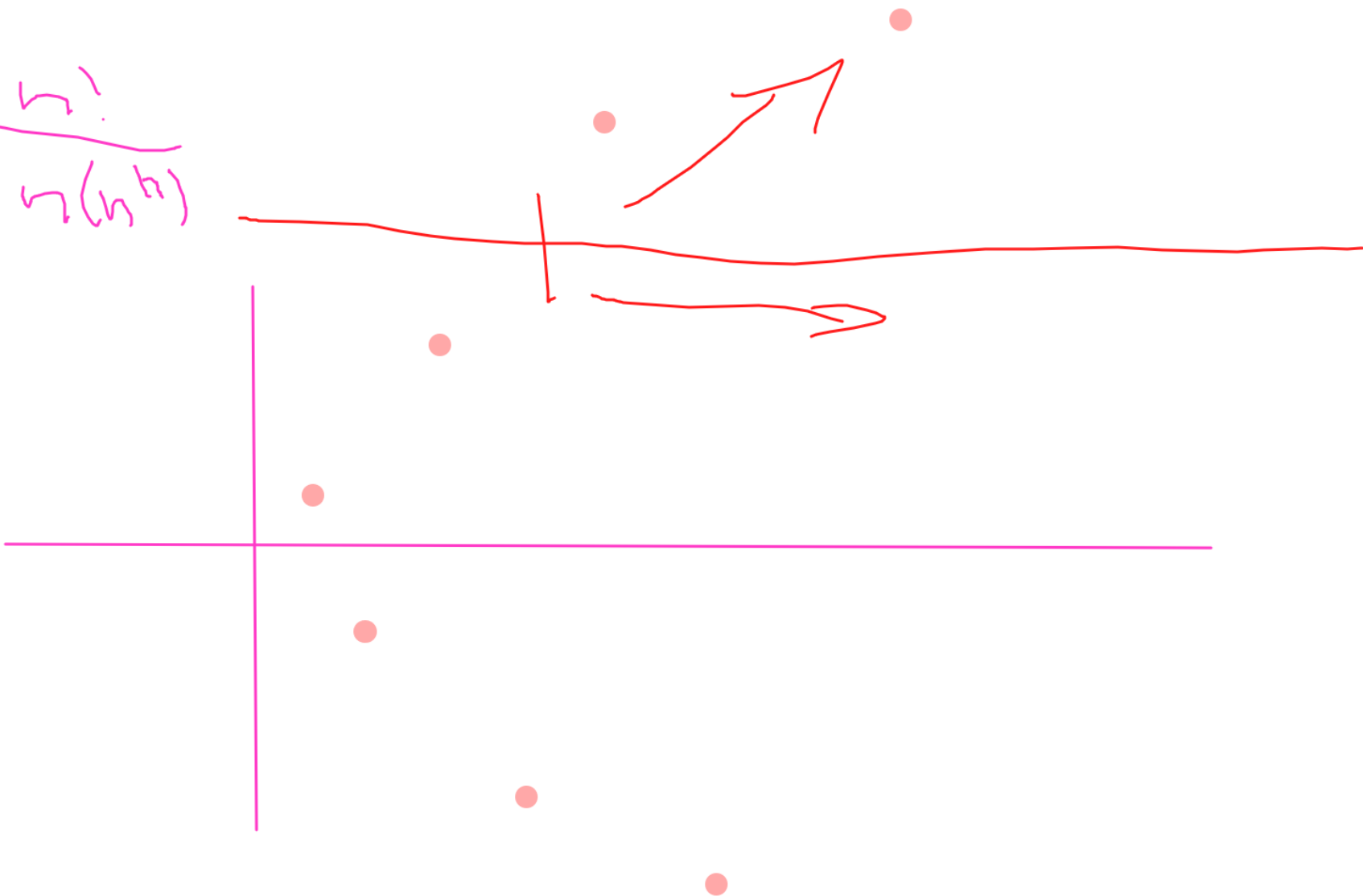


$$\lim_{n \rightarrow \infty} \frac{\sin(n!)}{n}$$

$$0 \leftarrow -\frac{1}{n} \ll \frac{\sin(n!)}{n} \ll \frac{1}{n} \rightarrow 0$$

$$\lim \frac{n!}{\sin(n^n)}$$



$$\lim_{n \rightarrow \infty} \frac{5 \cdot 2^n + n^8}{5^n + 10n^2}$$

$$= 0$$

$\ll \lim_n$

$$\frac{5 \cdot 2^n}{5^n} + \frac{n^8}{5^n} \rightarrow 0$$
$$\frac{1}{5} + \frac{10}{5^n} \rightarrow 0$$

$\rightarrow 0$

$$1 = \lim_{n \rightarrow \infty} 1 = \lim_{n \rightarrow \infty} \frac{h}{n} \stackrel{!}{=} \lim_{n \rightarrow \infty} n \cdot 0 = \lim_{n \rightarrow \infty} 0 = 0$$

$$\lim_n \left(\sqrt{1 + \frac{1}{n}} - \sqrt{1 - \frac{1}{n}} \right) =$$

$$\lim_n \left(\frac{\sqrt{1 + \frac{1}{n}} - \sqrt{1 - \frac{1}{n}}}{1} \cdot \frac{\sqrt{1 + \frac{1}{n}} + \sqrt{1 - \frac{1}{n}}}{\sqrt{1 + \frac{1}{n}} + \sqrt{1 - \frac{1}{n}}} \right) =$$

$$= \lim_n \frac{\left(1 + \frac{1}{n}\right) - \left(1 - \frac{1}{n}\right)}{\sqrt{1 + \frac{1}{n}} + \sqrt{1 - \frac{1}{n}}} \stackrel{\lim_{n \rightarrow \infty}}{=} \lim_{n \rightarrow \infty} \frac{\cancel{2} \cdot \frac{1}{n}}{\cancel{2} + \sqrt{\quad}} = \lim_{n \rightarrow \infty} \frac{1}{2} = \boxed{1}$$

\uparrow 0 0 \uparrow

$$\lim_{n \rightarrow \infty} \frac{\log_2(n)}{n} = \lim_{n \rightarrow \infty} \frac{\frac{\log_n n}{\log_n 2}}{n} = \lim_{n \rightarrow \infty} \frac{1}{n \log_n 2}$$

$$\log_n 2 = \frac{\ln 2}{\ln n} \rightarrow 0$$

$$n = 2^k \quad n \rightarrow \infty \Leftrightarrow k \rightarrow \infty$$

$$\lim_{n \rightarrow \infty} \frac{\log_2(2^k)}{2^k} = \lim_{k \rightarrow \infty} \frac{k}{2^k}$$

$$\lim_{n \rightarrow \infty} \sqrt[n]{n} = \lim_{n \rightarrow \infty} e^{\frac{1}{n} \ln(n)} = e^{\lim_{n \rightarrow \infty} \frac{\ln(n)}{n}} = e^0 = 1$$

$$\lim_{n \rightarrow \infty} \frac{\sqrt{16 - \frac{1}{n}} - 2}{\sqrt{16 - \frac{1}{n}} - 4} = \lim_{n \rightarrow \infty} \frac{(16 - \frac{1}{n}) - 4}{(\sqrt[4]{16 - \frac{1}{n}} + 2)}$$

$$\lim_{n \rightarrow \infty} \sqrt[4]{16 - \frac{1}{n}} - 2$$

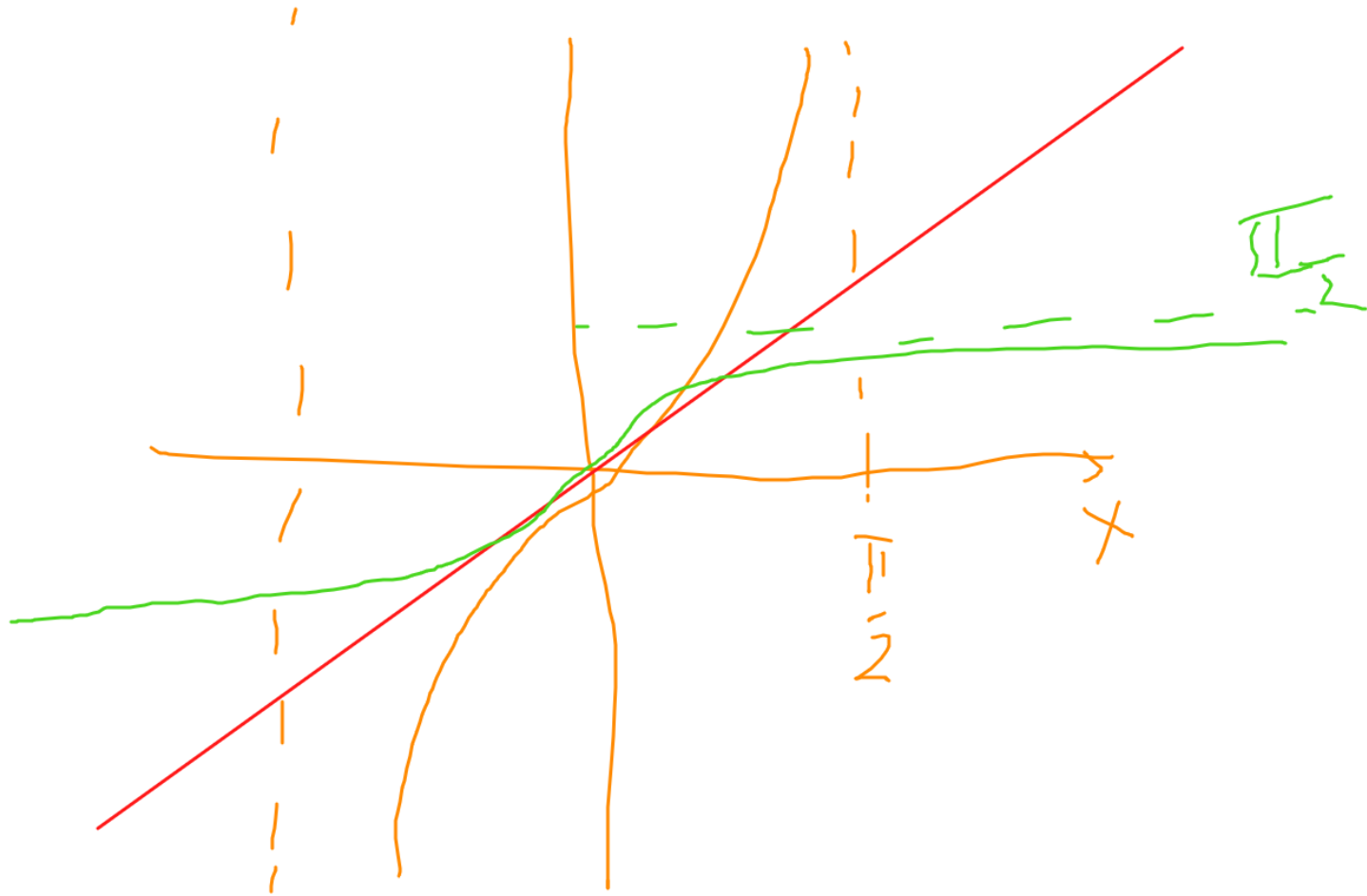
$$\sqrt[4]{16 - \frac{1}{n}} - 4$$

$$= \lim_{n \rightarrow \infty} \frac{(16 - \frac{1}{n}) - 4}{()}$$

$$= \frac{\sqrt[4]{a} - \frac{2}{\sqrt{a}}}{\sqrt{a} - \frac{4}{\sqrt{a}}}$$

$$\sqrt[4]{16 - \frac{1}{n}} - 2$$

$$\frac{\sqrt[4]{16 - \frac{1}{n}} - 2}{(\sqrt[4]{16 - \frac{1}{n}} + 2)(\sqrt[4]{16 - \frac{1}{n}} - 2)} = \frac{1}{2+2} = \frac{1}{4}$$



$$\frac{de^a}{da} = e^a$$

$$\frac{dN}{dt} = +RN$$

SIR

$$N = S + I + R$$

$$\frac{ds}{dt} = -RIS$$

$$\frac{dI}{dt} = +RIS - \alpha I$$

$$\frac{dR}{dt} = +\alpha I$$

