

$$a \in \mathbb{R}$$

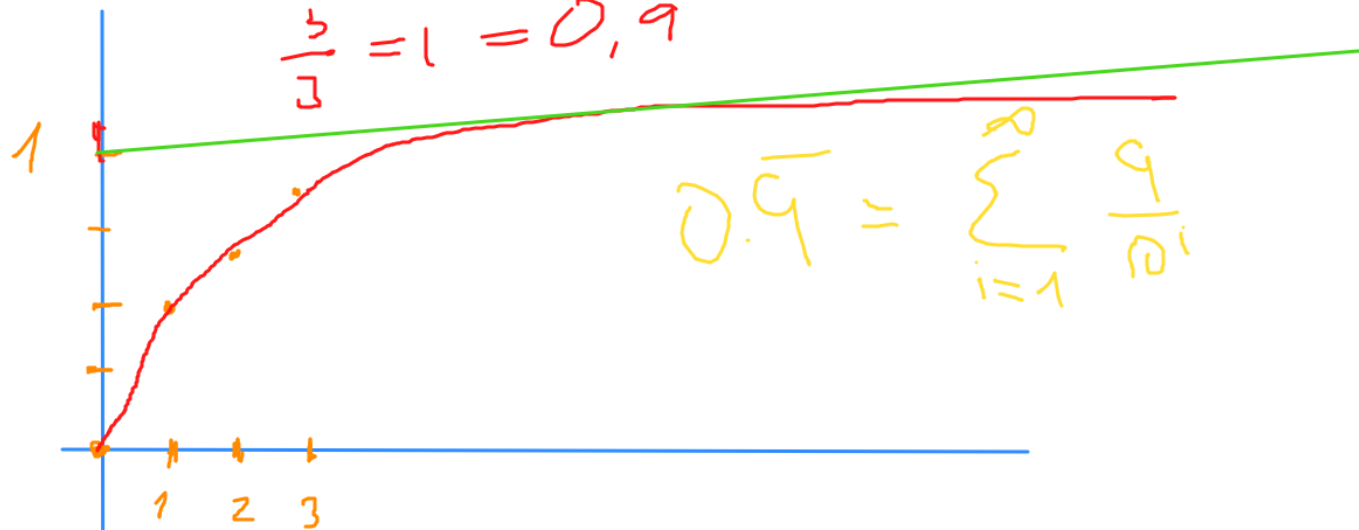
$$\exists x \in \mathbb{R} : f(x) = a$$

$$f\left(\frac{1-a}{2}\right) = \dots > a$$

$$\frac{1}{3} = (0, \overline{3}) \quad / \cdot 3$$

$$\frac{3}{3} = 1 = 0, \overline{9}$$

$$0, \overline{9} = \sum_{i=1}^{\infty} \frac{9}{10^i}$$



$$\min f(x) = 0 = \inf f(x)$$

$$\max f(x) \text{ does not exist.}$$

$$\sup f(x) = 1$$

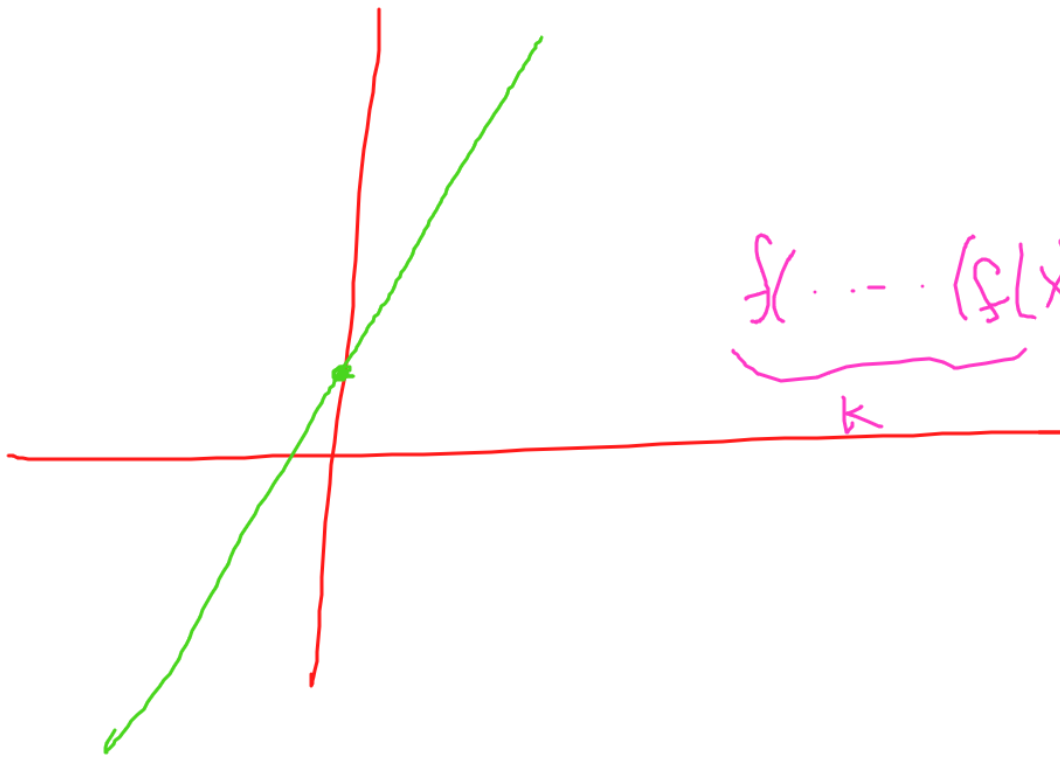
$$f(x) = \frac{x}{1+x}$$

$$= \frac{1+x-1-x+x}{1+x}$$

$$= 1 + \frac{-1-x+x}{1+x}$$

$$= 1 - \frac{1}{1+x}$$

$$a \in [0, 1) \Rightarrow \exists x_a \in \mathbb{R}_0^+ : f(x_a) = a$$



$$f(f(x))$$

$$= f(2x+1) = 2(2x+1)+1 = 4x+3$$

$$f(y) = 2y+1$$

$$\underbrace{f(\dots(f(x))\dots)}_k = 2^k(x+1) - 1$$