Arrays

- ... when we need to store many elements of the same type (e.g., 1 000 of integer numbers),
- they get defined in the section of variables (i.e., var)),
- they get defined using the keyword array, followed by an interval that defines its bounds, and the underlying data-type.
- Example: <u>var</u> a: array [1..100] <u>of</u> integer; file_example:array[5..50] of string;
- Individual members are accessed using square brackets: Example:

```
a[1]:=10;
file_example[6]:='xxx';
{Beware:} file_example[1]:='out of bounds!';
```

Sieve of Eratosthenes

```
var primes: array[2..1000] of boolean;
                                               i,j:integer;
begin
for i:=2 to 1000 do primes[i]:=true;
for i:=2 to 1000 do
begin
      if primes[i] then
       begin writeln(i,' is a prime');
             i:=2:
             while(i*j <= 1000) do
             begin
                    primes[i*i]:=false;
                    i := i + 1;
             end;
       end:
```

Programování I

Searching in an array

- Unsorted array ⇒ simple upper and lower bound (pass through the whole array until found),
- sorted array:
 - unary search (browse through the array like through a book),
 - binary search (start in the middle, in each step halve the input),
 - quadratic search, generalized quadratic search...

Unary search

- Simple algorithm, simple analysis, its complexity:
- lacksquare $\Theta(n)$.

Binary search

- What's the complexity of the algorithm? When do we have to add an extra step?
- lacksquare $\Theta(\log n)$.

Further examples

of array manipulation algorithms and complexity analysis:

- Matrix-multiplication:
- Naive algorithm Easily implementable, simple complexity-analysis.
- Strassen's algorithm hard to implement, hard to analyze, hard to understand, but it has a better complexity.
- Coppersmith-Vinograd's algorithm yet even more complicated with yet better complexity.
- Finding the largest zero-submatrix:
- Naive algorithm: $O(n^6)$
- Any ideas how to beat this complexity?
- Exercise (think about it at home, a solution will be shown later).

Horner's Method

- We want to convert a number stored as a string into an integer.
- Naive approach: We may start from the least important digit, keep track of an exponent by 10 and sum up.
- ... or we use Horner's method and start with the most important digit.
- We find its value and proceed (inductively): Multiply so far obtained result by 10 and add (sum up with) the newly loaded digit.

Number $a_n a_{n-1} a_{n-2} ... a_0$ in decimal (position) system means: $a_n 10^n + a_{n-1} 10^{n-1} + ... + a_0$. It holds:

$$a_n 10^n + a_{n-1} 10^{n-1} + \dots + a_0 = (\dots((a_n * 10) + a_{n-1} * 10) + \dots + a_1) * 10 + a_0$$

In the same way we may evaluate numbers in other position

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```
program x;
var a:string;
    i, value: longint;
begin
     readln(a); i:=1; value:=0;
     while i <= length(a) do
     begin
          value:=10*value+ord(a[i])-ord('0');
          i:=i+1;
     end;
     writeln(value);
end.
```

Evaluating a polynomial

- Consider a polynomial $a_n x^n + a_{n-1} x^{n-1} + ... + a_0$.
- We want to evaluate it, i.e., find its value for some value of x.
- Possibilities?
- Brute force (estimate $a_n x^n$, $a_{n-1} x^{n-1}$,... and sum it up)
- or Horner's method:

$$\sum_{i=0}^{n} a_i x^i = ((...(a_n x + a_{n-1})x + ... + a_1)x + a_0).$$

- 1: Read the coefficient of highest (so far not processed) monomial
- multiply the value obtained so far with x,
- add the value of the newly read coefficient,
- GOTO 1:

```
program nothing;
var i,a,sum,degree,x:integer;
{Evaluate a polynomial for a value x, use variable a
to read the coefficients}
begin
      readln(degree); readln(x);
      sum:=0;
      for i:=0 to degree do
      begin sum:=sum*x;
            readln(a);
            sum:=sum+a;
      end;
      writeln('The value is: ',sum);
end.
```

Excursion – labels and GOTO

- It is possible to perform hard-wired jumps within a Pascal program.
- After defining the global variables (section var) we can define a section label. There we list the used labels.
- Then we may use these labels in the program
- and by goto label; we perform a jump to the location of the label.
- Never use GOTO (in structured programming). I am using it in pseudocode in order to postpone the introductin of loop constructs after the kernel of the algorithm.

Defining functions and procedures

- Often the same sequence of nontrivial operations will be needed in many different places (and it would be inefficient to write them more than once).
- Procedures and functions provide us with a possibility to define such sequences once and using (calling) them many times.
- Procedures are a part of a program. Procedures are able to process parameters passed to them.
- Functions are a part of a program. They are able to process given parameters and to return a result.
- Examples: Cross the street; write out a message; arrive somewhere (by a train); calculate a factorial...

Defining a function

function name(argument :type;...):type_of_result

- Start with keyword function followed by name of the function.
- arguments are listed in parentheses (as if we defined variables).
- Inidividual arguments get separated by a semicolon (while defining).
- After a colon we put the type of the result.
- Value of the result gets assigned into a special variable with the same name as the function has.

```
program x;
var a:integer;
function sum_up(a:integer; b:integer):integer;
begin
        sum_up:=a+b;
end;
begin
        a:=sum\_up(5,10);
        writeln(a);
end.
```

Local variables

- Each function may use special variables (its own).
- These variables are called the *local* variables.
- We define them in a normal way, just their definition appears after the header of a particular function-definition:
- function f(a:integer):boolean; var b,c:integer;... begin...end;

```
function sum_up(a:integer; b:integer):integer;
var c:integer;
begin
        c:=a+b;
        sum_up:=c;
```

end;

Note that the variable used to define the result is write-only. It must **never** be read! (It could not be distinguished from calling a parameter-less function.)

Scope resolution

- In addition to global variables there are also so called *local* variables.
- Local variables are visible only within the appropriate functions.
- A local variable may have the same name as a global one.
- In case of such a conflict, inside the function only the local variable is visible.
- Values of the parameters are (by default) a value-parameters, i.e., the value of an expression is copied. If the function changes this value, this change is not propagated to the caller.

Reference-parameters

Sometimes we want to propagate the argument-change to the caller. How can we do that?

We use the keyword var in the appropriate place:

Result: 5 and 0; only genuine variables can be passed as such parameter!

Parameter-free functions

It can make sense to define functions without parameters (e.g., a function reading the data).

Then we omit parentheses behind the function-name (when, both, defining and calling it):

```
function x:integer;
begin
    x:=10;
end;
...
a:=x;
```

Procedures

```
'Procedures are functions that return no value.'
procedure name(arguments);
      name(arguments);...
example:
procedure writeit(a:integer;b:integer);
begin
      writeln(a); writeln(b);
      {We output the parameters}
end;
... writeit(5,10);...
```

Nested Functions and Procedures

```
It is possible to define a function inside another one:
    procedure f(a:integer);
        procedure g(b:integer);
        begin
            writeln('Proc. g in proc. f w/arg. ',b);
        end;
    begin
        writeln('Procedure f with argument ',a);
        g(2);{Calling nested proc. g}
end;
```

Scope resolution

- Procedure can 'see' (except of local variables) also local variables of its parents.
- Conflicting names resolve to the most 'local' one.
- In this way we can define 'local' procedures and functions. I.e., nested functions that are visible only inside their direct parents (not from grand-parents and further).

```
procedure f(h:integer);
    procedure g(b:integer);
        procedure h(c:integer);
        begin
            writeln('Procedure h with arg. ',c);
        end;
    begin
        writeln('Procedure g with arg. ',b);
        h(5);
    end;
begin
    writeln('Procedure f with arg. ',h);
    g(3); f(5); {so far so good, but calling
         h(4) here causes an error!
```