

```

with(simplex) :
P := {x5 = -0.5 x1 + 5.5 x2 + 2.5 x3 - 9 x4, x6 = -0.5 x1 + 1.5 x2 + 0.5 x3 - x4, x7 = 1
      - x1}:
f := 10 x1 - 57 x2 - 9 x3 - 24 x4:
print( `maximalizuj f` = f); print( `za podmienok` ); for e in P0 do e; end do;
print( `x1,...,x7` ≥ 0);
      maximalizuj f = 10 x1 - 57 x2 - 9 x3 - 24 x4
      za podmienok
      x5 = -0.5 x1 + 5.5 x2 + 2.5 x3 - 9 x4
      x6 = -0.5 x1 + 1.5 x2 + 0.5 x3 - x4
      x7 = 1 - x1
      0 ≤ x1,...,x7

```

(1)

```

P0 := P;
f0 := subs(P0, f) :
for e in P0 do e; end do; print( `-----` ); z = f0;
      x5 = -0.5 x1 + 5.5 x2 + 2.5 x3 - 9 x4
      x6 = -0.5 x1 + 1.5 x2 + 0.5 x3 - x4
      x7 = 1 - x1
      -----
      z = 10 x1 - 57 x2 - 9 x3 - 24 x4

```

(2)

Pivotovacie pravidlo "najväčší koeficient" vyberie do bázy x1, Blandovo pravidlo tiež. Urobíme teda pivotovací krok s x1, z bázy vystúpi x5:

```

P1 := pivot(P0, x1, pivoteqn(P0, x1)) :
f1 := subs(P1, f0) :
for e in P1 do e; end do; print( `-----` ); z = f1;
      x1 = -2 x5 + 11 x2 + 5 x3 - 18 x4
      x6 = 1 x5 - 4 x2 - 2 x3 + 8 x4
      x7 = 1 + 2 x5 - 11 x2 - 5 x3 + 18 x4
      -----
      z = -20 x5 + 53 x2 + 41 x3 - 204 x4

```

(3)

Najväčší koeficient: x2

Blandovo pravidlo: x2

```

P2 := pivot(P1, x2, pivoteqn(P1, x2)) :
f2 := subs(P2, f1) :
for e in P2 do e; end do; print( `-----` ); z = f2;
      x1 = 0.75 x5 - 2.75 x6 - 0.50 x3 + 4.00 x4
      x2 = -0.25 x6 + 0.25 x5 - 0.50 x3 + 2.00 x4
      x7 = 1.00 - 0.75 x5 + 2.75 x6 + 0.50 x3 - 4.00 x4
      -----
      z = -6.75 x5 - 13.25 x6 + 14.50 x3 - 98.00 x4

```

(4)

Najväčší koeficient: x3

Blandovo pravidlo: x3

$P3 := \text{pivot}(P2, x3, \text{pivoteqn}(P2, x3)) :$

$f3 := \text{subs}(P3, f2) :$

for e in P3 do e; end do; print(' ----- '); $z = f3;$

$$x2 = 2.5 x6 - 0.5 x5 + 1.0 x1 - 2.0 x4$$

$$x3 = -2.0 x1 + 1.5 x5 - 5.5 x6 + 8.0 x4$$

$$x7 = 1.0 - 1.0 x1$$

$$z = 15.0 x5 - 93.0 x6 - 29.0 x1 + 18.0 x4$$

(5)

Najväčší koeficient: x4

Blandovo pravidlo: x4

$P4 := \text{pivot}(P3, x4, \text{pivoteqn}(P3, x4)) :$

$f4 := \text{subs}(P4, f3) :$

for e in P4 do e; end do; print(' ----- '); $z = f4;$

$$x3 = 2.00 x1 - 0.50 x5 + 4.50 x6 - 4.00 x2$$

$$x4 = -0.50 x2 + 1.25 x6 - 0.25 x5 + 0.50 x1$$

$$x7 = 1.00 - 1.00 x1$$

$$z = 10.50 x5 - 70.50 x6 - 20.00 x1 - 9.00 x2$$

(6)

Najväčší koeficient: x5

Blandovo pravidlo: x5

$P5 := \text{pivot}(P4, x5, \text{pivoteqn}(P4, x5)) :$

$f5 := \text{subs}(P5, f4) :$

for e in P5 do e; end do; print(' ----- '); $z = f5;$

$$x4 = 1.5 x2 - 1.0 x6 + 0.5 x3 - 0.5 x1$$

$$x5 = -2.0 x3 + 4.0 x1 + 9.0 x6 - 8.0 x2$$

$$x7 = 1.0 - 1.0 x1$$

$$z = -21.0 x3 + 22.0 x1 + 24.0 x6 - 93.0 x2$$

(7)

Najväčší koeficient má x6, Blandovo pravidlo by vybralo x1, keďže má najmenší index.

Teraz budeme pokračovať podľa pivotovacieho pravidla "najväčší koeficient",

k Blandovému pravidlu sa vratíme neskôr.

$P6 := \text{pivot}(P5, x6, \text{pivoteqn}(P5, x6)) :$

$f6 := \text{subs}(P6, f5) :$

for e in P6 do e; end do; print(' ----- '); $z = f6;$

$$x5 = 2.5 x3 - 0.5 x1 - 9.0 x4 + 5.5 x2$$

$$x6 = -1.0 x4 + 1.5 x2 + 0.5 x3 - 0.5 x1$$

$$x7 = 1.0 - 1.0 x1$$

$$z = -9.0 x_3 + 10.0 x_1 - 24.0 x_4 - 57.0 x_2 \quad (8)$$

$P7 := pivot(P6, x_1, pivoteqn(P6, x_1)) :$

$f7 := subs(P7, f6) :$

for e in P7 do e; end do; print(' ----- '); $z = f7;$

$$x_1 = -2 x_5 + 11 x_2 + 5 x_3 - 18 x_4$$

$$x_6 = 8 x_4 - 4 x_2 - 2 x_3 + 1 x_5$$

$$x_7 = 1 + 2 x_5 - 11 x_2 - 5 x_3 + 18 x_4$$

$$z = 41 x_3 - 20 x_5 + 53 x_2 - 204 x_4 \quad (9)$$

Keď si však vypíšeme tabuľku v kroku 1, zistíme, že je rovnaká:

for e in P1 do e; end do; print(' ----- '); $z = f1;$

$$x_1 = -2 x_5 + 11 x_2 + 5 x_3 - 18 x_4$$

$$x_6 = 1 x_5 - 4 x_2 - 2 x_3 + 8 x_4$$

$$x_7 = 1 + 2 x_5 - 11 x_2 - 5 x_3 + 18 x_4$$

$$z = -20 x_5 + 53 x_2 + 41 x_3 - 204 x_4 \quad (10)$$

Algoritmus sa dostal do rovnakého stavu, v akom bol v kroku 0. Keďže je deterministický, znamená to, že sa zacyklil.

Teraz sa skúsime vrátiť do kroku 6, kde miesto pravidla "najväčší koeficient" použijeme Blandovo pravidlo (teda pivotovací krok spravíme s x_1 miesto x_6):

$P6b := pivot(P5, x_1, pivoteqn(P5, x_1)) :$

$f6b := subs(P6, f5) :$

for e in P6b do e; end do; print(' ----- '); $z = f6b;$

$$x_1 = -2 x_4 + 3 x_2 - 2 x_6 + x_3$$

$$x_5 = 2 x_3 - 8 x_4 + 4 x_2 + 1 x_6$$

$$x_7 = 1 + 2 x_4 - 3 x_2 + 2 x_6 - 1 x_3$$

$$z = -9 x_3 + 10 x_1 - 24 x_4 - 57 x_2 \quad (11)$$

$P7b := pivot(P6b, x_3, pivoteqn(P6b, x_3)) :$

$f7b := subs(P7b, f6b) :$

for e in P7b do e; end do; print(' ----- '); $z = f7b;$

$$x_1 = 1 - 1 x_7$$

$$x_3 = -1 x_7 + 1 + 2 x_4 - 3 x_2 + 2 x_6$$

$$x_5 = -2 x_7 + 2 - 4 x_4 - 2 x_2 + 5 x_6$$

$$z = -1 x_7 + 1 - 42 x_4 - 30 x_2 - 18 x_6 \quad (12)$$

Konečne nám stúpla účelová funkcia na 1 a vidíme, že všetky premenné v z majú

záporné koeficienty, takže sme dosiahli optimum.