#### Algorithmic game theory

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12th lecture

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Source: youtube.com

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- In general single-parameter environments, we use Myerson's lemma.

# Revenue maximizing auctions



Source: Reprofoto

# Revenue maximization

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Source: https://merger.com/recurring-revenue/

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• The situation then becomes more complicated, but we will see some nice results today.

• Consider single-item auction with 1 bidder with valuation v.



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- the only DSIC auction: the seller posts a price r, then his revenue is either r if  $v \ge r$  and 0 otherwise.
- Maximizing the social surplus is trivial by putting r = 0.
- However, when maximizing the revenue, it is not clear how we should set *r*, since we do not know the valuation *v*.

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Source: https://goodgearguide.com.au

# Reserve price and maximizing revenue

#### Reserve price and maximizing revenue

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#### Reserve price and maximizing revenue

- The theory was developed by Roger Myerson.
- Very roughly, if the seller believes that bidders have high valuations, he should set a high reserve price accordingly.



Source: https://www.science4all.org/article/auction-design/

### Optimal auctions more generally

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• There are also optimal DISC auctions even if we relax the conditions by not insisting on  $F_1, \ldots, F_n$  being identical. However, optimal auction can get weird, and it does not generally resemble any auctions used in practice.



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  - $\circ~$  Oral exam with preparation, 3 hours max.
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- What you should know: everything that we covered (everything is included in the lecture notes).





Thank you for your attention.