

# Algorithmic game theory

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# Other notions of equilibria

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- The solution concept of correlated equilibria (CE) is more promising as it can be found efficiently.

# Regret minimization

## Example

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## No Regret Learning (review)

No single action significantly outperforms the dynamic.

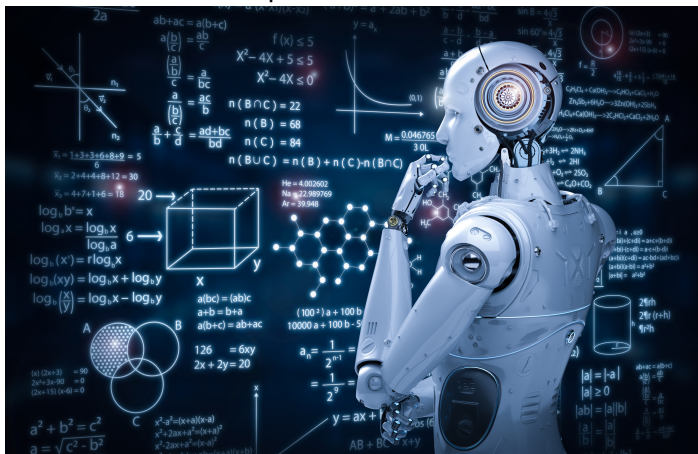


<b>0</b>	<b>1</b>
<b>1</b>	<b>0</b>

Weather					Loss
Algorithm					<b>1</b>
Umbrella					<b>1</b>
Sunscreen					<b>3</b>

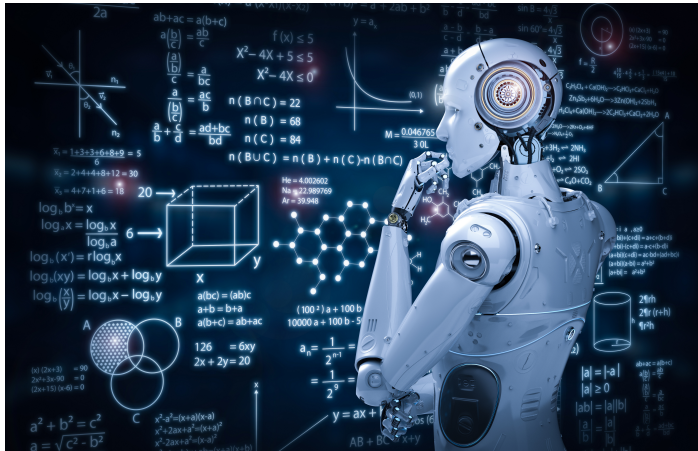


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Sources: <https://clubitc.ro>

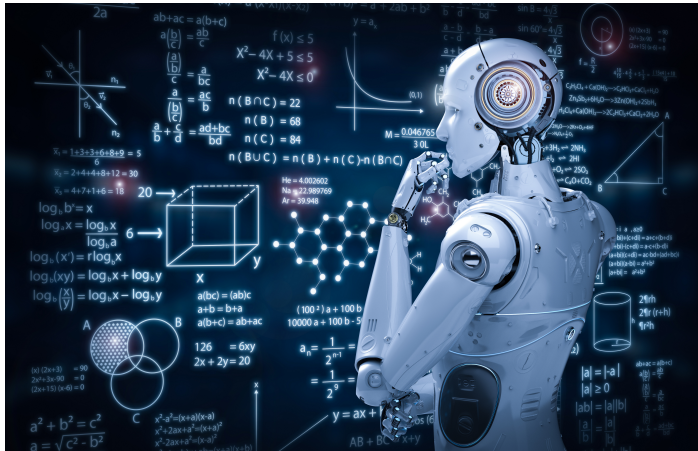
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Thank you for your attention.