Overview

- Structures (record data type),
- Binary files,
- Simple sorting algorithms,
- Units.

Record data type

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- Thus we define a structure. There we can keep related data "together".
- We use a keywork `record` to define a structure.

The record data type definition

examples and syntax

```
type  point=record
            x,y:integer;
      end;
var   a,b:point;
      book:record
            author:  string[100];
            title:  string[100];
            year:  integer;
      end;
```

Accessing the structure elements

We use a binary (infix) operator " ." to access a structure element:
`a.x` – member `x` in a structure (record) `a`
Individual members behave as variables thus we may read their value, assign a value...
Note that we may pass them as an argument by reference!

The record data type

example

```
var a,b:point; boo:book;
begin
      a.x:=1;
      a.y:=2;
      b.x:=10;
      b.y:=10;
      boo.author:='Mehlhorn, K.';
      boo.title:='Data Structures and Efficient
Algorithms I';
      boo.year:=1984;
end.
```

Array of structures

```
var library:array [1..100] of record
            author:string[25];
            title:string[45];
            year:integer;
end;
begin
      for i:=1 to 100 do begin
            readln(library[i].author);
            readln(library[i].title);
            readln(library[i].year);
      end; ...
```

Keyword `with`

While working with structures, it can be inefficient always having to name the underlying structure whose members we use (e.g., `a_structure_with_a_long_name_that_we_though_out_after_drinking`
Thus we may write:

`with` structure do statement or block;

and in the statement (or block) we need not to mention the structure explicitly (we may use them directly).

Construction with

an example

```
procedure output(book_with_a_long_name:book);
begin
      with book_with_a_long_name do
            writeln(author:25,name:46,year:5);
end;
...
      for i:=1 to 100 do
            output(library[i]);
...
```

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- Text files are nice, but from time to time we want to implement, say, a database (e.g., library).
- Now we need a file with completely different properties – mainly we want to be able to access (quickly) the kth element (and edit it).
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- We define a file consisting of many elements of a given type (e.g., structure (record)).

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- Differences:
  - `filesize` – returns a number of elements (records) in the file
  - `seek` – puts a pointer to the given point (size says of how many elements of our type the file consists).

Example

a phone book

```
type entry=record
       name:string[100];
       number:string[20];
end;
var f:file of entry;
```

Inserting...

... into a binary file

```
procedure add;
var ent:entry;
begin readln(ent.name);
      readln(ent.number);
      assign(f,'database.bin');
      {$I-}
      reset(f);
      {$I+}
      if IOResult<>0 then
            rewrite(F);
      seek(f,filesize(f));
      write(f,ent);
      close(f);
end;
```

Writing the file out

i.e., reading the whole file...

```
procedure output;
var i:integer;
    ent:entry;
begin
      assign(f,'database.bin');
      reset(f);
      for i:=1 to filesize(f) do
      begin
            read(f,ent);
            writeln('Name:  ',ent.name,', phone nr: '
,ent.number);
      end;
      close(f);
end;
```

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Function `truncate`

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- similarly with `rewrite(f);`, just for a nonexistent file the program would crash!
- How to erase one entry?
- Replace it with the last one and truncate (the last one).

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back to structures

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- Examples: Library, phone book, accounting records,...
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- Example: A journal has no author, book has no program committee...
- How can we organize a library consisting of books, journals and newspapers?
- We use so called **variant record.**
- We define the attributes depending on an indicator variable.

Syntax

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- Then we define a structure where we cover this type by the case-clause:

```
type tbook=record
    name:string;
    pagenum:integer;
    case type:typeofbook of
        book:  (author:string);
        journal:  (editorinchief:string;
            color:boolean);
        newspaper:  (neditorinchief:string;
            spam_volume:real;);
    end;
```

Example

Library

```
var library:array[1..100] of tbook;
begin
      library[1].name:='Data Structures and
Algorithms I';
      library[1].pagenum:=226;
      library[1].type:=book;
      library[1].author:='Kurt Mehlhorn';

      library[2].name:='40Hex';
      library[2].pagenum:=30;{I guess...}
      library[2].type:=journal;
      library[2].editorinchief:='Darkangel';
      .....
```

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- Data in the variant part are stored in a *union*, *i.e.*, they are stored one over another! Languages from the C family call it `union`.
- Variant records are an ancient ancestor of polymorphism and inheritance that are implemented in object languages.
- Object programming will be covered at the beginning of the summer term.

Sorting – the motivation

- We have read the data,
- we want to process it in a monotone ordering.
- How to do that? Sort, process.
- Let us consider data that has been read into an array.

The problem of sorting – simple sorting algorithms

- BubbleSort,
- InsertSort,
- SelectSort,
- QuickSort.

Bubblesort

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- The idea: We are comparing pairs of consecutive numbers from the first pair to the last one. If they are incorrectly ordered, we swap their positions.
- Individual elements are "bubbling" in a correct direction.
- We iterate this process until no swap takes place.

Bubblesort in pseudocode

```
weswapped:=true;
while weswapped do
begin
    for i:=1 to length - 1 do
    begin
        weswapped:=false;
        if numbers[i]>numbers[i+1] then
        begin swap(numbers[i],numbers[i+1]);
              weswapped:=true;
        end;
    end;
end;
```

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- Thus it suffices to perform at most n iterations. Complexity of one iteration is also linear ($O(n)$).
- Thus altogether $O(n^2)$.
- We may implement the algorithm when in odd iterations we bubble from left to right while in even iterations from right to left. This is called **Shakesort**. Its complexity is the same.

Insert- and Select-sort

Selectsort:

- Repeat until the array to sort is empty:
- Find a minimum in the array to sort and add it to the sorted array.

Insertsort:

- Repeat until the array to sort is empty:
- Take the first element of the array to sort and place it onto the correct position in the target array, i.e.:
  find the position where this element should be in the target array, add it there and the rest of the target array move one position further.

Complexity-analysis: We iterate the process $n$times. One iteration takes at most cn steps (for some constant c). Therefore altogether $O(n^2)$.

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- Divide the array A into arrays B and C. B consists of the elements smaller than p, C consists of elements larger than p.
- Employ recursion on B, employ recursion on C
- Output the array B, output pivot p (as many times as it was in A), output C.

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- Altogether, again, $O(n^2)$.
- The average-case complexity is $\Theta(n \log n)$ and the algorithm can be improved to gain this complexity by choosing pivot in a smarter way.
- To improve this algorithm we want to find a median - but we have to do it in linear time.

FIXME!!!

Here shall be a remark on method "Divide et impera"!
Here should be a quicksort implementation!
Passing a function as an argument.
Odstrasujici priklady (slidy10.tex for mathematicians).

Units

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- We may copy (click'n'paste) them into the other source files (bad idea)
- or we store them into a separate file that gets compiled separately.
- The latter approach is referred as the **units.**

Units – advantages and disadvantages

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- Source code gets stored into several files,
- it is not necessary to replicate the code if we want to share it in several projects.

Units – syntax and semantic

- Instead of word `program` we start with keyword `unit`,
- after this we place the name of the unit. This time the name must correspond with the filename. Also the keyword `unit` is compulsory.
- A unit consists of an `interface` (what's visible from the outside)
- and of `implementation` (internal part where the interface is implemented).

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- function (and proc.) prototypes (when the function should be publicly visible),
- prototype is the header of the function, i.e., the "first line".

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- definition of any stuff that should be (publicly) invisible,
- definition of internal functions (not mentioned in interface).
- We finish the unit by keyword `end.` (followed by full-stop)

Units – example

```
unit sorting;
interface
      type po=array[0..9] of integer;
      procedure bubble(var arr:array of integer);
      procedure select(var a:po);
      procedure insert(var a:po);
      procedure quicksort(var arr:array of
integer;number:integer);
      procedure output(a:array of integer);
```

Units – example (cont.)

```
...
implementation
      var inserted:integer;
      procedure bubble(var arr:array of integer);
      ...
      function extract_min(var a:po):integer;
      {This function will not be visible from
outside!}
      ...
      procedure select(var a:po):integer;
      ...
      ...
end.
```

Units – how to use them

- When using a unit, we announce it with a keyword `uses` followed by the name of the unit:
- Example: `uses sorting;`

Using the unit – example

```
program sort;
uses sorting;
var p:array [0..9] of integer;
i:integer;
begin
for i:=0 to 9 do
read(p[i]);
quicksort(p,10);
output(p);
end.
```

Standard units

Turbo Pascal is equipped with several standard units:

- crt,
- dos,
- graph,
- printer,
- ...

Units may differ for individual compilers!

Unit `crt`

- Unit operating a keyboard and a display (colors, sounds)
- Variables: `LastMode` (says what textmode was the last one used before switching graphics on),
- `TextAttr` (current attributes for displaying (text). Gets operated by `TextBackground` and `TextColor`),
- Procedure `TextBackground` sets the background color, proc. `TextColor` sets the color of foreground.
- function `keypressed` (returns `boolean` saying whether any key was pressed, `clrscr` (erases the display).

Units dos, graph a printer

- Unit `dos` works with files, directories, disks...
- Unit `graph` enables graphic mode (`InitGraph`, `CloseGraph`, `GraphResult`, `SetColor`, `GetColor`...).
- Unit `Printer` serves for printing.
- All these units consist of many functions, procedures and variables. If you want to, you may find them in Help.

Strange example:

Probably you have already seen this several times:

```
program nothing;
uses crt;
...
begin
...  repeat until keypressed;
end.
```

What is this?

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```
program nothing;
uses crt;
...
begin
...  repeat until keypressed;
end.
```

What is this?

Use of unit `crt`, namely its function `keypressed`.

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- This directive is placed after the function prototype:
- `procedure two(a:integer);forward;`

Forward example:

```
program qq;
procedure two(a:integer);forward;
procedure one(a:integer);
begin
      two(a);
end;
procedure two(a:integer);
begin
      one(a);
end;
begin
      one(1);
      {Let us ignore that this program does
not make a good sense!}
end
```