## Flows and cycles in graphs – Exercises 8

1. For a graph G (not necessarily cubic!) prove, that G has a 3-CDC if and only if G has a 4-NZF.

2. Prove the parity lemma directly; that is without using flows.

**3.** Let  $G_1$ ,  $G_2$  be cubic bridgeless graphs. Prove that  $G_1 \oplus_3 G_2$  is a snark if and only if one of  $G_1$ ,  $G_2$  is a snark.